# AN ADDENDUM TO "QUADRATIC FORMS OVER POLYNOMIAL EXTENSIONS OF RINGS OF DIMENSICN ONE"' 

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In Theorem 3.3 the condition that disc $q$ is extended from $R$ is redundant in view of the following:

Proposition. Let $R$ be a reduced commutative Noetherian ring of dimension one in which 2 is invertible and which has finite normalisation. Then the inclusion $R \hookrightarrow R\left[X_{1}, \ldots, X_{n}\right]$ induces an isomorphism $\operatorname{Disc} R \leadsto \operatorname{Disc} R\left[X_{1}, \ldots, X_{n}\right]$.

To prove the proposition we need the following:

Lemma. Let $R$ be any commutative ring in which 2 is a non-zero divisor; then $\mu_{2}(R)=\mu_{2}(R[X])$.

Proof. Let $f=a_{0}+a_{1} X+\cdots+a_{r} X^{r} \in \mu_{2}(R[X])$. Then the equation

$$
\left(a_{0}+a_{1} X+\cdots+a_{r} X^{r}\right)^{2}=1
$$

gives $a_{0}^{2}=1$ and hence $a_{0}$ is in $\mu_{2}(R)$. Let, if possible, $i>0$ be the least integer such that $a_{i} \neq 0$. Then $2 a_{0} a_{i}=0$ which implies that $a_{i}=0$, a contradiction. Thus $f=a_{0}$.

Proof of the proposition. Let $\bar{R}$ be the integral closure of $R$ in its total quotient ring and $c$ be the conductor of $R$ in $\bar{R}$. We then have the following commutative diagram of exact sequences:

where the vertical maps are induced by inclusions and $X$ denotes the tuple $\left(X_{1}, \ldots, X_{n}\right)$. Since $\bar{R}$ is a product of Dedekind domains and $\operatorname{dim} R / c=\operatorname{dim} \bar{R} / c=$ $0, i_{1}, i_{2}, i_{4}$ and $i_{5}$ are isomorphisms. Thus, by the five-lemma $i_{3}$ is an isomorphism.

In view of this, Corollary 3.5 should read as $W(R[X]) \rightrightarrows W(R)$.

